## Topic 7: Probability

### 1) The Basics of Counting:

## a) Fundamental Principle Of Counting:

If one event has  ${\bf m}$  possible outcomes and a second event has  ${\bf n}$  possible outcomes, then there are  ${\bf m} \times {\bf n}$  total possible outcomes for the two events together.

e.g. 2 starters and 5 main courses => 10 possible dinner options

### b) A Deck Of Cards:

- 52 Cards in a deck
- 4 suits: Spades & Clubs (black), Hearts & Diamonds (red)
- Picture Cards: Jack, Queen and King in each suit (12 in total)

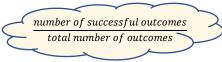
### c) Different Strategies:

- 1) We can simply list all possible outcomes.
- 2) We can make out a **two-way table**, if there are more than two trials
  - e.g. tossing a coin two or more times
- 3) Sometimes it can be useful to make out a **tree diagram**, for showing all possible outcomes of two or more trials.
- e.g. chance of picking one yellow and a blue bead from a bag of 6 yellow, 5 blue

## 2) Basics of Probability:

# a) Definition of Probability:

The probability of an event occurring is:

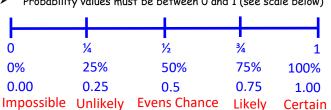


e.g. bag with 5 red and 4 green beads

$$P(Green) = \frac{4}{9}$$

#### Note:

Probability values must be between 0 and 1 (see scale below)



## b) Terminology:

- 1. Trial: doing an experiment in probability e.g. tossing a coin
- 2. **Outcome:** one of the possible results of the trial e.g. a 6 when throwing a die
- 3. Sample space is the set of all possible outcomes in a trial.
- 4. **Event** is the occurrence of one or more specific outcomes.
- 5. **Probability** is the measure of the chance of an event happening.

## c) Relative Frequency and Carrying Out Experiments:

- We can carry out an experiment or trials to estimate the probability of an event occurring.
  - e.g. throwing a die to see how many 6's we get
- If you throw a die 20 times and a 6 comes up 3 times we could estimate the probability of throwing a 6 to be  $\frac{3}{20}$ .
- This estimate we get from carrying out trials, is called the Relative Frequency.
- More trials are done => closer the rel freq and probability.

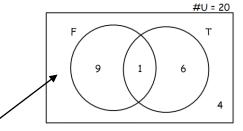
## 3) Set Theory and Probability:

### Notes:

- Sets can be used to help solve probability problems.
- Remember that  $A \cap B$  represents A AND B whereas  $A \cup B$  represents A OR B.

<u>Example 1:</u> 20 people asked if they preferred Facebook or Twitter. 10 said Facebook, 7 said Twitter and 4 said neither. Person selected at random from the group...what is the probability that the person selected: i) chose Facebook and Twitter ii) chose Facebook or Twitter iii) chose Facebook only?

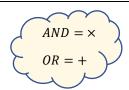
- Firstly, we need to draw a Venn Diagram to represent the problem.
- 4 people chose neither => 16 people chose Facebook or Twitter
- As 10 chose Facebook and 7 chose Twitter => 1 person chose both
- The Venn Diagram for this problem is shown on the right.



- i) P(Chose Facebook AND Twitter) =  $F \cap T = \frac{1}{20}$
- ii) P(Chose Facebook OR Twitter) =  $F \cup T = \frac{16}{20} = \frac{4}{5}$
- iii) P(Chose Facebook Only) =  $\frac{9}{20}$

# 4) Combined Events:

### Remember:



Example 1: Probability of Paul scoring a free throw is 0.8. What is the probability of:

- i) scoring three free throws in a row ii) scoring the first and missing the next two iii) scoring two of the three free throws?
- i) P(Score 1<sup>st</sup> AND Score 2<sup>nd</sup> AND Score 3<sup>rd</sup>) =  $0.8 \times 0.8 \times 0.8 = 0.512$
- ii) P(Score 1st AND Miss 2nd AND Miss 3nd) =  $0.8 \times 0.2 \times 0.2 = 0.032$
- iii) P(Score  $1^{st}$  and  $2^{nd}$  AND Miss  $3^{rd}$ ) OR (Miss  $1^{st}$  AND Score  $2^{nd}$  AND  $3^{rd}$ ) OR (Score  $1^{st}$  AND Miss  $2^{nd}$  AND Score  $3^{rd}$ ) =  $(0.8 \times 0.8 \times 0.2) + (0.2 \times 0.8 \times 0.8) + (0.8 \times 0.2 \times 0.8) = 0.128 + 0.128 + 0.128 = 0.384$